Habitat Loss, Uneven Distribution of Resources and Fragmented Landscapes—A Resource Based Model of the Patch Size Effect

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Abstract

The problem of habitat fragmentation is recently an important issue in ecological research as well as in the practical approach of nature conservation. According to the most popular approaches, habitats are considered as the homogenous parts of the landscape. Also the metapopulation concept problem of the inert habitat heterogeneity is considered quite seldom. These approaches have some weak points resulting from the assumption that the border between habitat patches and the metapopulation matrix is fairly sharp. This paper presents a resource-based concept of habitats, based on mathematical theory of point processes, which can be easily applied to analysing the problem of uneven distribution of resources. The basic assumption is that the random distribution of resources may be mathematically described as the realisation of a certain point process. According to our method, it is possible to calculate the expected quantities of available resources as well as the minimum area of habitat that includes the expected abundance of the resource. This approach may be very useful to understand some crucial phenomena in landscape ecology, such as the patch size effect and its connection to habitat loss and fragmentation.

Keywords

Patch Size Effect, Allee Effect, Habitat Loss, Habitat Fragmentation, Poisson Process, Process Intensity, Critical Patch Size

1. Introduction

A number of researchers [1]-[3] regard a far-reaching fragmentation of habitats to be one of the most important
challenges faced by theoreticians and practitioners of nature conservation. Most of the natural and—in recent decades—semi natural habitats, have been reduced to fragments of various size separated by roads, compact build-up areas or cultivated fields [4] [5]. The effects of such transformations exceed, markedly, the simple reductions in the size of population areas or changing the structures of existing metapopulations [6]. However quality of the fragmented habitat may be analysed with different assumptions which require a new approach and investigative tools [7] [8].

In recent two decades, a number of theories have been developed in spatial population dynamics [9]-[11]. Most of these theories have been based on Levin’s [12] model of metapopulation dynamics and assume that the space consists of finite number of homogeneous patches, surrounded by empty matrix. It is a major simplification, as a result of which the models have been judged as largely unrealistic and have received significant criticism. More realistic models, not assuming the homogeneity of the habitat patches, were presented by Day and Possingham [13], Frank and Wissel [14], Hanski and Ovaskainen [15] [16]. In some of these models, the matrix has no longer been treated as homogeneous, but showing e.g. dispersible areas and barriers. Equally important is the fact that these models, called stochastic patch occupancy models (SPOM) take into account another feature important for the realism of the model, i.e. stochasticity. Hanski [17] distinguishes two types of stochasticity, which affect population dynamics—demographic stochasticity, including: reproductive parameters, mortality, migrations and environmental stochasticity, including: weather conditions, partial destruction of the habitat, habitat fragmentation. Among all these factors, the broadly defined habitat loss or deteriorating habitat quality. The population dynamics models, that take into account the shifts in habitat quality, are presented by Possingham and Noble [18] and Akceakaya and Ferson [19], but they are criticized for their excessively many untested assumptions and a large number of parameters that are difficult to estimate [17].

Anyway, ecologists and conservation biologists have used many measures of landscape structure, to predict the population dynamics consequences of habitat loss and fragmentation [20]. Even though the aforementioned models placed significant emphasis on the functioning of the whole metapopulation system, they also considered, to a lesser or greater extent, the patch size effect (PSE), associated with fragmentation or, simply, reduction of the patch area. The ample empirical data show that the densities of populations living in small patches of habitat are lower than those from large-size habitats [21]. This phenomenon is well known to naturalists, although explaining its mechanisms has sometimes not been easy [22]. There are generally two ways of explanation. According to the first one, the PSE is the result of the set of intrapopulation disorders observed in small populations and empirically described as so-called “Allee effect” [23]-[25]. The second approach is concentrated on the space-related environmental changes. Relatively well recognized within this approach is the issue of “edge effect” [26], with the main considerations pertaining to aspects of the metapopulation [27]. Another concept assumes that with the progress of fragmentation, a major depletion of available resources can occur, although this has been relatively poorly researched [28].

Many populations are ultimately limited by resources, and their abundance and distribution will determine the carrying capacity of an environment [29]. If these resources are not distributed evenly in the habitat, the loss of territory may lead to a disproportionately greater loss of the resources [30]. In a way, this assumption concurs with the practice of estimating randomly distributed resources. For several dozen years, the amounts of such resources have been estimated by extrapolating the results of small, representatively distributed study plots, onto the whole area under consideration [31]. Similar techniques also provide a basis for contemporary research, but the extrapolation process now takes into account the “edge effects” [26] and influences of the of neighbouring habitats [32].

The extrapolation models are not particularly good in dealing with the fact that a random distribution of resources is, by definition, uneven [31]. Thus, when we divide a large area into several smaller ones, the required resources will almost certainly not be equally abundant in each part. Therefore, reliable modelling of the fragmentation process needs to solve both problems, namely the amount and distribution of resources. When the resources are not distributed randomly, but are associated with any easily distinguishable element of the habitat, e.g. river as a source of food and water, the situation is obvious. Any fragment without access to this resource (river) is useless to organisms which require permanent access to this resource e.g. amphibians. The situation becomes more complicated when the resources occur more or less randomly, and this situation seems to occur often. For example, the populations of cambiophages depend on the presence of weakened or wounded trees, which are randomly distributed throughout forests [33]. The situation becomes even more complicated, when limiting factors involve several resources that are strictly limited in terms of places of occurrence, such as in the
case of *Maculinea* butterflies, which require food-plants and host-ant’s nests [34]. The aim of this study is to demonstrate that where there is a random distribution of resources, the effects of fragmentation can be successfully predicted by using the point processes theory [35][36].

The suggested approach is based on the assumption that the random distribution of resources may be mathematically perceived as a realisation of certain point process, e.g. Poisson process. In estimating therefore the intensity of the process, we can learn about the expected occurrence (number, quantity) of a given resource in the selected area. Consequently, we can also calculate the probability that the resource occurs in the given area. Moreover, we can also calculate the probability of the resource occurring in the given area in sufficient quantity to maintain minimum viable populations of certain species. Consequently, one may try to reliably determine the minimum areas required for viable populations. This mathematical tool may be crucial for the process of the locating and size optimisation of protected areas. The methods of estimating the intensity of the Poisson process were described at length by Ripley [37]. Possible applications of the point processes have been recently presented in landscape planning and nature conservation by Grabarnik and Sarkka [38], who used those techniques for modelling the spatial structure of the forest, and in the field of random geometric graphs by [39]-[43].

In this paper we would like to present the possibility of using point process in the more general resource-based analysis of the habitat loss mechanism.

2. Method

2.1. Point Processes

Let us denote a certain stochastic environment called state space by *S* (**Figure 1**). This set may represent a certain defined area for example forest or meadow. Let us denote by *D* a certain sub area of *S* where we conduct our observations called observation space. Let us assume that the area *S* is an open terrain sowing by seeds of anemochorous plants. Other examples are the locations of birds’ nests, rocks, or towns. Of course, none of these is actually a point, but in each case the sizes of the objects are so small compared with the distances between them, that their size may be ignored [37]. Thus, seedlings appear in area *S*. One may try to describe such a process of sowing by giving the locations of particular seedlings treated as points on a plane. In practice it would be a long and laborious process because of the huge number of seedlings and the time which would be needed to search through the whole study area. Another way may involve the description via the number of points in selected parts of the observation space. We should call this space a sample space *B*. A detailed description of the scenery may be obtained by counting the frequency of points *x*_1, ..., *x*_n in subsets *B* of *D*.

The experimental plots established in standard ecological studies are a particular example charged with additional assumptions [37] [44]. Let us assume that we observe *n* different points within the measurable state space *S* and the order of outcome is of no interest. Therefore, space *B* may be represented by the set *B* = *x*_1, ..., *x*_n — also called configuration. If we allow only the countable configurations, then for any configuration *x* : *i* ∈ *I*, *I* ⊂ *N* we can rewrite the number of points *x* _i_ belonging to *B* ∈ *B* , where *B* is the Borel *σ*-field on *S* by

\[
\mu(\cdot) = \sum_{i \in I} \delta_{x_i}(\cdot)
\]  

where *δ* _x_ ( *B* ) is Dirac measure with mass 1 at *x**, being defined on *B* by

![Figure 1. The example of certain two-dimensional point process with state space S, observation area D and sample set B. Black points represent the distribution of seedlings.](image-url)
Such a discrete measure $\mu$ is called a point measure. As each configuration has a certain corresponding point measure, we thus consider a space of point measures on $\mathcal{B}$ denoted by $\mathcal{M} = \mathcal{M}(S, \mathcal{B})$. Since $\mu$ may be identified with $(\mu(B))_{B \in \mathcal{B}}$, it is justified calling the mapping

$$\pi_B : \mathcal{M} \ni \mu \mapsto \pi_B(\mu) := \mu(B)$$

(3)
a projection or coordinate function with index $B$. Let $\mathcal{E} = \mathcal{E}(S, \mathcal{B})$ be the smallest $\sigma$-field introduced on $\mathcal{B}$ such that the projections $\pi_B$, $B \in \mathcal{B}$ are measurable. $\mathcal{E}$ is the $\sigma$-field generated by sets of the form

$$\pi_B^{-1}(c), \ c \subset \mathbb{N}_0 = \{0,1,2,\ldots\}$$

(4)

Let us now assume that the number and positions of the points may be random. Let $(\Omega, \mathcal{F}, P)$ be the probability space on which the random variables are defined. Elements of $\Omega$ will be denoted by $\omega$. A mapping

$$N : \omega \in \Omega \rightarrow N(\omega, \cdot) \in \mathcal{M}(S, \mathcal{B})$$

(5)
is called a point process on $(S, \mathcal{B})$, if it is measurable with respect to $\mathcal{E}$ and $\mathcal{E}(S, \mathcal{B})$. In other words, point process is a random point measure on the state space $(S, \mathcal{B})$, i.e. such a measure, that for each set $B \in \mathcal{B}$, the number of points $N(B)$ which occurred in this set is a random variable.

We know that any set $B$ being a subset of the observation space $D$, may be described using the random variable $N(B)$, which represents the number of points in the set $B$. Thus, the random variable $N(B)$ may be treated as a composition of the point process $N$ and the projection $\pi_B$ (Figure 2).

As we mentioned earlier, point process is a random point measure on the state space $S$. Let us now define a certain non-random measure for the point process, called intensity. Intensity measures play an important role in the characterisation of point processes. The intensity $\nu$ of a point process $N$—also called mean measure is defined by the expectations

$$\nu(B) = EN(B), \ B \in \mathcal{B}$$

(6)

Hence, $\nu(B)$ is the expected number of points in set $B$.

### 2.2. Poisson Process with a Finite Intensity Measure and Distribution of Resources

The basic point process is a Poisson process. Poisson processes are very convenient building blocks from which to generate other point processes. They can be regarded as the analogue of independent observations and are often called “random” outside mathematics [37].

Let $\nu$ be a finite intensity measure on the state space $(S, \mathcal{B})$. The point process $N$ is a Poisson process, when satisfies the following properties: for each set $B \in \mathcal{B}$, the number of points $N(B)$ in set $B$ has a Poisson distribution with the parameter $\lambda = \nu(B)$ and the variables $N(B_1), N(B_2), ..., N(B_k)$ are independent.
random variables for each natural \( k \) and any pairwise distinct \( B_1, B_2, \ldots, B_k \in \Omega \).

Let us consider a vast open terrain, homogeneous in terms of its characteristics, such as, for example a muddy and dried bed of a shallow lake, and the locations of independently wind propagating seeds of one species selected from those colonising the area. The number of seeds which fall on one square metre of the area is a variable with Poisson distribution, which stems from the fact that there are many such seeds, each with little probability of landing on the marked square \([44]\). We may therefore, safely assume that the distribution of cells in the bed is a realisation of the Poisson process with intensity \( \lambda \).

### 2.3. Distribution of Resources and Patch Size Effect

Let us assume that the distribution of resources is a realisation of a certain Poisson process with the parameter \( \lambda = v(B) \). We can therefore, calculate the probability of occurrence of the resource \( k \) times in the selected area \( B \) using the Poisson distribution probability mass function

\[
P(k, \lambda) = \frac{(\lambda^k |B|)^k}{k!} e^{-\lambda|B|}
\]

(7)

Obviously, the process does not have to have a constant measure of intensity, as the latter may change, for example, with the lapse of time

\[
\lambda_{t_1,t_2} = \int_{t_1}^{t_2} v(t) \, dt
\]

(8)

In such a case, the probability of the resource occurring \( k \) times on the selected area \( B \) within the time period \((t_1, t_2)\), expressed as \( N(t_2) - N(t_1) \) is

\[
P(N(t_2) - N(t_1) = k) = \frac{(\lambda_{t_1,t_2} |B|)^k}{k!} e^{-\lambda_{t_1,t_2} |B|}
\]

(9)

The intensity of a process can also depend on position, which in fact, is commonly seen in biology e.g. we can expect that number of seedlings decrease with distance from the plant producing wind dispersing seeds (Figure 3). In such a case, the probability of hitting exact quantity of recourse is equal to

\[
P(N(B) = k) = \frac{\left( \int_{\Phi} \lambda(x) \, dx \right)^k}{k!} e^{-\int_{\Phi} \lambda(x) \, dx}
\]

(10)

For the sake of simplification, in the following parts of this study, we will consider processes with a constant intensity measure \( \lambda \).

![Figure 3. The intensity of a process can also depend on position \( \lambda = \lambda(x) \) e.g. number of seedlings decrease with distance from the plant producing wind dispersing seeds.](image)
3. Results

3.1. Habitat Loss and Patch Size Effect

Let us consider a situation where one resource \( R \) limits the possibility of persistence of a certain species within a certain area \( S \). The lack of the resource or an insufficient quantity means that the species cannot persist in the area \( S \). We also assume that the limiting resource \( R \) is randomly distributed on the area \( S \) and that the minimum amount of the resource is \( R_{\min} = 1 \). This assumption, although biologically questionable, was introduced for the mathematical clarity of the argument. Further parts of this paper will present subsequent steps that bring the model closer to reality. The probability of the PSE occurrence in the area \( S \) is thus equal to the probability of finding \( k = 0 \) resources in the area, and we can calculate it using (7)

\[
P_{\text{PSE}}(k = 0, \lambda) = e^{-\lambda}
\]  

By using (7) we can present the relationship between the size of the area \( S \) and the probability of occurrence of PSE in the area as a function of the intensity of process \( \lambda \). Figure 4(a) presents the relationship between the probability of PSE occurrence and the percentage decrease of the habitat area size, for three intensity levels: \( \lambda = 1 \), \( \lambda = 4 \) and \( \lambda = 10 \).

3.2. Number and Quantity of Resources and Patch Size Effect

In biological examples, however, the key is often not the occurrence of the resource alone, but also that it occurs in certain quantities. The example of such a situation could be the presence of shoots of a host plant required to maintain the assumed population abundance of an insect [45]. In the suggested approach, the interpretation of such a case is a situation where a greater number of resource occurrence is required \( R_{\min} > 1 \), and the probability of the occurrence of PSE, is equal to the sum of probabilities of the occurrence of smaller quantities of the resource \( R \) being smaller than required

\[
P_{\text{PSE}} = \sum_{k=0}^{k=R_{\min}-1} P(k, \lambda)
\]  

Hence, when the occurrence of the given species is only possible when the given resource occurs in the defined area a minimum of three times, the probability of PSE occurring is equal to

\[
P_{\text{PSE}} = P(k = 0, \lambda) + P(k = 1, \lambda) + P(k = 2, \lambda)
\]  

The relationship between the probability of PSE occurrence and the percentage decrease in habitat area size, for three intensity levels: \( \lambda = 1 \), \( \lambda = 4 \) and \( \lambda = 10 \), in the situation where the minimum amount of the resource needed for the population to stay is \( R_{\min} = 3 \), is presented in Figure 4(b).

![Figure 4. The probability of the PSE occurrence (P) depending on the percentage loss of area S, for the assumed process intensities \( \lambda = 1 \), \( \lambda = 4 \) and \( \lambda = 10 \). (a) Minimum quantity of resources \( R_{\min} = 1 \); (b) Minimum quantity of resources \( R_{\min} = 3 \).](image)
Let us have a closer look at the relationship between the intensity of the process and the minimum amount of the resource and their effects on probability of the PSE occurrence (Figure 5(a)). It can been clearly seen that the less intensive the process, the higher the probability of the PSE occurrence, even for low values of minimum resource quantity. The higher the $\lambda / R_{\text{min}}$ ratio, the lower the probability of the PSE occurrence (Figure 5(b)).

The theory of point processes may be also applied in the analysis of availability of a number of different resources—which is, in biological terms, much closer to the real situation. Let us consider the simplest situation, where we have two resources $R_1$ and $R_2$ that are limiting the possibility of persistence of a certain species in the area $S$. Let $R_{\text{min}}$ represent a minimum quantity of resource $R_1$, $\lambda_1$—the intensity of the process describing the distribution of the resource $R_1$, $R_{\text{min}}^2$—a minimum quantity of resource $R_2$ and $\lambda_2$—the intensity of the process describing the distribution of the resource $R_2$. The species could remain in the area $S$ only when both resources occur in suitable quantities. The PSE will occur when at least one of the required resources occurs in a quantity smaller than required. The possibility of PSE occurring is therefore equal to:

$$P_{\text{PSE}} = P(P_{\text{PSE}}|P_{\text{PSE},1})P_{\text{PSE},1} + P(P_{\text{PSE}}|P_{\text{PSE},2})P_{\text{PSE},2}$$

where $P_{\text{PSE},1}$ is the probability of the PSE occurrence, as a result of an insufficient number of occurrences of the resource $R_1$, $P_{\text{PSE},2}$ is the probability of the PSE occurrence as a result of an insufficient number of occurrences of resource $R_2$ calculated using (7).

### 3.3. Critical Patch Size

The crucial question at the patch scale is how much habitat must be conserved to ensure the persistence of populations [46]. The best-known models for critical patch size are KISS models [47] and Skellam [48]. In current usage, a KISS model is generally interpreted as a reaction-diffusion equation for a population density on a bounded region, with the coefficients of the equation being constant in the region and the density falling to zero on the boundary of the region [49]. An example that we shall address in the present article is critical patch size and its connection to the distribution of resources. Using the point processes theory, we can calculate the minimum size of the habitat patch, where the quantity of resources needed to support a population is to occur with a certain level of probability.

**Example**

Let us assume that the persistence of a certain population in the area $S$ is limited by a certain resource $R$. Let us also assume that the distribution of this resource is a realisation of a certain Poisson process with an intensity $\lambda$. By reformulating (7) we can calculate the minimum area $B$ (as a fraction of the area $S$) on which, with a certain defined probability $P$ and given intensity $\lambda$, the given resource will occur at least once

$$B = \frac{1}{\lambda} \ln P_{\text{PSE}}$$

**Figure 5.** The influence of the Poisson process intensity and minimum quantity of resource (a) and of the ratio $\lambda / R_{\text{min}}$ (b) on the probability of the PSE occurrence.
Let us illustrate this with a simple example (Figure 6). Let us assume that our state space $S$ is an area of 10 hectares. The minimum quantity of the limiting resource $R$ required by the species is $R_{\text{min}} = 1$. Because the resource $R$ occurs nineteen times in the area $S$, we assume that the expected quantity of resource (Poisson process intensity) is $\lambda = 19$. Let us assume that we are interested in such a minimum size for patch $B$, on which the resource occurs with the probability of $P = 0.95$. Therefore, probability of the PSE occurrence is equal to $P_{\text{PSE}} = 1 - P$. Substituting these values into (15) we obtain $B = 0.1576$. It means that the minimum area of the patch where we can observe at least one resource, with the probability of $P = 0.95$ is 0.1576 of the area $S$, which, in our case, means that the minimum area of the patch $B$ is 1.576 hectares.

4. Conclusion—Consequences for Practice

One of the most important aspects of practical nature conservation is to establish protected areas whose objective is to preserve naturally a considerable level of biological diversity, as well as the natural characteristics of ecological processes [50] [51]. So far theoretical aspects of the relationship between the patch size and the level of biodiversity it harbours have been discussed in detail [50] [52]-[56]. However, the issue of minimum area necessary to maintain a viable population of a certain species is still a topic of discussion. Because of the widespread occurrence of the phenomenon, a number of studies have focused on the relationships between habitat patches [3] [14] [20] only marginally treating the issue of single patch size. On the other hand, the IUCN guidelines on the planning of protected areas, recommend that they should possibly cover rather large areas. In a number of studies on the planning of protected areas, the area of a habitat is seen as a kind of indirect measure of population abundance [57] [58]. However, in the case of the diversified internal structure of a habitat, this assumption may lead to the occurrence of serious artifacts, which were theoretically and empirically demonstrated by [59]. The use of knowledge rooted in the theory of point processes, as suggested in this study, allows one to determine the probability of a decrease in the availability of resources in tandem with the diminishing habitat patch size. This approach offers an objective way to find the level of threat in different variants of decreasing area size. The question still to be answered is, which level of probability may provide a basis for creating reliable models of the effect of decreasing patch size, upon the availability of resources and hence on the status of the populations depending on them. The approach proposed in this paper offers only answers concerning the decrease in resources. This situation is analogous with the results of population vulnerability analysis (PVA), which determine the probability of extinction of the population within a certain time [60]-[63]. The levels of probability of extinction at which monitoring or protective actions should commence, largely depend on arbitrary decisions depending on the importance of the species, the global status of the threatened species, as well as other detailed factors [64] [65]. The possibility of practical use of the point processes theory, in finding the biological consequences of fragmentation or designing protected areas, increases the widespread application of the GIS systems in these fields [66]-[68]. This can help in the development of tools permitting a more precise determination of the effects of disappearance or fragmentation of habitats, and prevention of the adverse effects of such processes.
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